

BASIC IDENTITIES

For each $x \in \mathbb{R}$ for which both members are defined:

1. $\tan x = \frac{\sin x}{\cos x}$
2. $\cot x = \frac{\cos x}{\sin x}$
3. $\sec x = \frac{1}{\cos x}$
4. $\csc x = \frac{1}{\sin x}$
5. $\cot x = \frac{1}{\tan x}$
6. $\sin^2 x + \cos^2 x = 1$
7. $1 + \tan^2 x = \sec^2 x$
8. $1 + \cot^2 x = \csc^2 x$
9. $\cos(x_2 \pm x_1) = \cos x_2 \cos x_1 \mp \sin x_2 \sin x_1$
10. $\cos(-x) = \cos x$
11. $\cos\left(\frac{\pi}{2} - x\right) = \sin x$
12. $\cos 2x = \cos^2 x - \sin^2 x = 2 \cos^2 x - 1 = 1 - 2 \sin^2 x$
13. $\cos \frac{x}{2} = \pm \sqrt{\frac{1}{2}(1 + \cos x)}$
14. $\sin(x_2 \pm x_1) = \sin x_2 \cos x_1 \pm \cos x_2 \sin x_1$
15. $\sin(-x) = -\sin x$
16. $\sin\left(\frac{\pi}{2} - x\right) = \cos x$
17. $\sin 2x = 2 \sin x \cos x$
18. $\sin \frac{x}{2} = \pm \sqrt{\frac{1}{2}(1 - \cos x)}$
19. $\tan(x_2 \pm x_1) = \frac{\tan x_2 \pm \tan x_1}{1 \mp \tan x_2 \tan x_1}$
20. $\tan(-x) = -\tan x$
21. $\tan 2x = \frac{2 \tan x}{1 - \tan^2 x}$
22. $\tan \frac{x}{2} = \frac{\sin x}{1 + \cos x}$
23. $\cos(\pi \pm x) = -\cos x$
24. $\sin(\pi \pm x) = \mp \sin x$
25. $\tan(\pi \pm x) = \pm \tan x$
26. $\cos(x_2 + x_1) + \cos(x_2 - x_1) = 2 \cos x_2 \cos x_1$
27. $\cos(x_2 + x_1) - \cos(x_2 - x_1) = -2 \sin x_2 \sin x_1$
28. $\sin(x_2 + x_1) + \sin(x_2 - x_1) = 2 \sin x_2 \cos x_1$
29. $\sin(x_2 + x_1) - \sin(x_2 - x_1) = 2 \cos x_2 \sin x_1$
30. $\cos x_1 + \cos x_2 = 2 \cos \frac{x_1 + x_2}{2} \cos \frac{x_1 - x_2}{2}$
31. $\cos x_1 - \cos x_2 = -2 \sin \frac{x_1 + x_2}{2} \sin \frac{x_1 - x_2}{2}$
32. $\sin x_1 + \sin x_2 = 2 \sin \frac{x_1 + x_2}{2} \cos \frac{x_1 - x_2}{2}$
33. $\sin x_1 - \sin x_2 = 2 \cos \frac{x_1 + x_2}{2} \sin \frac{x_1 - x_2}{2}$

